

1/3

.33

2/3

.66

1/6

.16

2/6

.33

5/6

.83

1/5

.2

$2/5$

.4

$3/5$

.6

$4/5$

.8

$1/8$

.125

$2/8$

.25

$3/8$

.375

$5/8$

$.625$

$6/8$

$.75$

$7/8$

$.875$

2^3

8

2^4

16

2^5

32

2^6

64

2^7

128

2^8

256

2^9

512

2^{10}

1024

3^3

27

3^4

81

4^3

64

4^4

256

5^3

125

5^4

625

6^2

36

7^2

49

8^2

64

9^2

81

10^2

100

11^2

121

12^2

144

13^2

169

14^2

196

15^2

225

16^2

256

17^2

289

18^2

324

19^2

361

20^2

400

$\sqrt{2}$

1.414

$\sqrt{3}$

1.732

$\sqrt{64}$

8

$\sqrt{121}$

11

$$\sqrt{144}$$

12

$$\sqrt{225}$$

15

$$\sqrt{400}$$

20

$$\sqrt{289}$$

17

$$\sqrt{324}$$

18

$$\sqrt{625}$$

25

$$\sqrt{900}$$

30

$$\sqrt{1024}$$

32

Real Numbers

all numbers on the
number line

Rational numbers

All numbers that can be
expressed as the ratio of
two integers (all integers
and fractions)

Irrational Numbers

all real numbers that are
not rational, both positive
and negative (e.g. Pi and
 $\sqrt{-x}$)

commutative law

Doesn't matter in what
order operation is
performed
– Addition
– Multiplication

Associative law

Terms can be regrouped with parenthesis without changing the result

Distributive law

allow to distribute a factor among terms being added or subtracted
 $a(b+c) = ab + ac$

Adding or subtracting fractions

have to have a common denominator

LCD

Least common denominator is the least common multiple of the denominator.

Multiplying fractions

just multiply top and bottom, but you can reduce the fractions diagonally first if possible

Compare fractions

Cross multiply to see which one is larger. Product relates to the one with numerator. So start with the numerator on the left.

First 25 prime numbers	2,3,5,7,11,13,17,19,23,29,31,37,41,43,47,53,59,61,67,71,73,79,83,89,97
Only even prime number?	2
Divisible by 2	Last digit is an even number > 0,2,4,6,8
Divisible by 3	Sum of all the digits is divisible by 3
Divisible by 4	last two digits of number are divisible by 4
Divisible by 5	0 or 5

divisible by 6

Divisible by 2 and 3 – sum of all the digits is divisible by 3, and the last digit is zero or an even number

Divisible by 7

double the value of the last digit and subtract the result from the rest of the number. The answer is divisible by

$$\begin{array}{l} 7? \\ 385 \\ 38 - (2 \times 5) = 28 \\ 28 / 7 = 4 \end{array}$$

Divisible by 8

Can be divided by 2 evenly 3 times – last 3 digits are divisible by 8?

Divisible by 9

sum of all the digits of the number is divisible by 9

LCM/LCD using prime factorization

ELIMINATE DUPLICATES and LEAVE HIGHEST POWER. Break down the numbers into prime factorization, then eliminate duplicates and leave only duplicates to the highest power, multiply together and you get the LCM/LCD

GCF

OVERLAP. Greatest common factor. The greatest integer that divides with no remainder into two or more given integers. Break down into prime factorization and then find the overlap.

Divide fractions?

multiply by the reciprocal

Sum of all positive integers up to and including 99

$(1+99)/2 = 50$ so you got the average of all numbers up to and including 99
Then you can multiply by number of numbers... 99
 $99*50 = 4950$

Number of 3 digit numbers?

$$999-100+1=900$$

Addition Odd and Even number behaviour?

Odd + Odd = EVEN
Even + Even = EVEN
Odd + Even = Odd

Subtraction Odd and Even number behaviour

Even - Odd = Odd
Even - Even = Even
Odd - Even = Odd
Odd - Odd = Even

Multiplication of odds and evens

Even * Even = Even
Even * Odd = Even
Odd * Odd = Odd

Divisible by 12

Divisible by 4 and by 3

Divisible by 15

Divisible by 5 and 3

Solving quadratic
equation $k^2 - 8k + 15 = 0$

Find what two numbers multiply to 15 and add to -8. so must be -5 and -3. So factor it out into $(k-5)(k-3) = 0$ so k can be either 5 or 3

DS - if one of the statements is equal to the one in the prompt then it confirms that the statement in the prompt is true. i.e. if it is a dependent formula then it doesn't help to solve for additional variables but will confirm that a statement is true. So if they say solve for x then it might not help but if they say does $kx=4 - mx$ and one of the statements is a dependent formula then it will help

If you add two numbers that have the same factor

The resulting number will also be divisible by that number

Pythagorean triples - 3 main ones

3-4-5 (and multiples, e.g. 6-8-10), 5-12-13, 7-24-25

Pythagorean triples

3-4-5, 5-12-13, 7-24-25,
8-15-17 (The longest side
is of course the one
opposite the 90 degree
angle)

Special right triangles
45-45-90

The sides are
proportional as $x-x-x$
($\sqrt{2}$)

Special right triangle
60-30-90

The sides are
proportional as $x-x$
($\sqrt{3}$)- $2x$ (the x is
opposite the 30)

Split an equilateral
triangle into 2?

you get 2 30-60-90
triangles!

If you have 2 of the
following points you can
solve for the rest

1. Length side 1
2. Length side 2
3. Length hypotenuse or
Diagonal of the square
4. Area
5. Perimeter

30/360

1/12

60/360

1/6

90/360

3/12 or 1/4

120/360

4/12 or 1/3

210/360

7/12

240/260

8/12 or 2/3

45/360

1/8

$$90/360$$

$$2/8 \text{ or } 1/4$$

$$135/360$$

$$3/8$$

$$180/360$$

$$1/2$$

$$225/360$$

$$5/8$$

Area of a sphere

$$4/3 \text{ Pi } r^3$$

Surface area of a sphere

$$4 \text{ pi } r^2$$

Formula to find sum of angles in a shape??

$(n-2) \times 180$ where n is the number of sides. Or you can count the triangles you can form within the shape and multiply by 180

Properties of a parallelogram

one pair of parallel sides and those sides are equal in length, if sides weren't equal in length would be a trapezoid.

What to do when you are solving an equation with absolute value and a variable outside of the absolute value sign?

e.g. $|x+4| = 4x+3$
you need to first solve for two answers, positive and negative $4x+3$, but then TEST BOTH ANSWERS, it could be that one doesn't work, this is key, especially for data sufficiency problems.

is 0 an integer?

yes

If question says sum of two primes is odd

Then one of them must be 2, because all other primes are odd and $O + O = E$. so only $E + O$ can equal O .

is 0 positive or negative?

neither

Mean and median in consecutive sets?

always equal to each other, and also both are equal to mean of first and last numbers. so you dont even need all the numbers of the set

When counting consecutive integers

ADD ONE BEFORE YOU'RE DONE!

ODD VS EVEN – median/ avg of a set with odd vs. even numbers?

even numbers then median is not an integer, odd elements then integer

The product of k consecutive integers, is always divisible by

$k! \dots K$ factorial.

Divisibility of sum of set with odd number of elements?

will be divisible by the number of elements

Divisibility of sum of set with even number of elements

will NOT be divisible by the number of elements. because the avg is not an integer if set has even elements. xxxx, no middle number!

$$1.4^2$$

2

$$1.7^2$$

3

$$2.25^2$$

5

$$30^2$$

900

$$25^2$$

625

If you add a non-multiple
of N to a multiple of N =

Non-multiple of N 18
(mult of 3) + 10 = 28
(non-mult of 3)

If you subtract a non-multiple of N from a multiple of N =

Non-multiple of N 30
(mult of 3) – 10 (non mul
of 3) =

How many factors does a perfect square have?

an ODD number of factors – because it has one "unpaired" factor which multiplies by itself to give the number, but the factor is only counted once!

How many factors does a non-perfect square have?

an EVEN number of factors – because it always has "paired" factors, 1 and itself, 2 and x, 3 and y etc.

Properties of the prime factorization of perfect squares?

there are only prime factors to even powers! of course because $3 \times 3 = 9$, so $3^2 \dots$ and $9 \times 9 = (3 \times 3)(3 \times 3) = 3^2 \times 3^2 = 3^4$

Properties of the prime factorization of a non-perfect square?

have prime factors to odd powers! i.e. may have prime factors to even powers but has one to odd power or all to odd power. Not all are to even power!

How many factors does 2000 have?

solve for prime fact $2^4 \times 5^3$ and then use counting principle $(4+1)(3+1) = 20$, the factors could have any combination of 2s, thus could have zero twos, one 2, two 2s, three 2s, or four 2s, so you multiply the possibilities of each factor by each other to get the number of possible combinations.

Write an even arbitrary number algebraically?

$$2n$$

write an odd arbitrary number algebraically?

$$2n + 1 \text{ or } 2n - 1$$

formula for change in mean if a new term is added?

distribute the weight of new term to each of total terms. i.e. (new term - average) / new total No. of terms

How many zeros at the end of 60!

Check how many 2s and 5s in the numbers prime factorization, i.e. how many times is it divisible by 10? so will be divisible by same number as lowest power of 2 and 5. (if prim fact contains 2^3 and 5^6 then it is div by 10^3 times). so 60 will be multiplied by 12 multiples of 5 ($5 \times 12 = 60$) and additionally 25 and 50 will have 2 fives in them, as 5×5 is 25 and $5 \times 2 \times 10$ is 50. so $12 + 2 = 14$ zeros!

A line that passes through the origin and point $(-a, -a)$ has a slope of?

$$1$$

A point that is reflected over the $y=x$ line?

switch around the x and y points. i.e $(2,3)$ on the other side of the line $y=x$ is $(3,2)$.. equidistant to the line $y=x$

Divisor

Doesn't mean only prime factors!! it means factors/divisors, so everything that will go into the number. i.e. for 12 it is 1,2,3,4,6,12

Linear equation of a line

$y=mx+b$ m is the slope and b is the Y intercept!!! so when x is zero, the line crosses the Y axis at B !!

how do you represent two numbers with reversed digits?

$10t+s$ and $10s+t$ then use these representations to get whatever it is you need

5×6

30

6×6

36

6×7

42

6x8

48

6x9

54

6x12

72

7x6

42

7x7

49

7x8

56

8x7

56

8x8

64

9x8

72

9x9

81

9x12

108

11x12

132

12x12

144

13x12

156

12*13

156

3x9

27

4x9

36

5x9

45

8x5

40

7x5

35

2x9

18

12x9

108

12x5

60

12x7

84

12x4

48

12x8

96