

Number System Practice Questions

Q1. If a, b, c and d are prime numbers such that $1 < a < b < c < d$ and $abcd = 1430$, then what is the value of d ?

- A) 3
- B) 9
- C) 11
- D) 13
- E) 22

Q2. What is the least positive integer that is divisible by each of the integers 1 through 7, inclusive?

- A) 420
- B) 840
- C) 1260
- D) 2520
- E) 5040

Q3. If x is equal to the sum of even integers from 40 to 60 inclusive and y is the number of even integers from 40 to 60 inclusive. What is the value of $x + y$?

- A) 550
- B) 551
- C) 560
- D) 561
- E) 572

Q4. If S is a set of four numbers w, x, y and z . Is the range of the numbers in S greater than 2?

- 1) $w - z > 2$
- 2) z is the least number in S

Q5. If a, b and c are integers, is the number $3(a + b) + c$ divisible by 3?

- 1) $a + b$ is divisible by 3
- 2) c is divisible by 3

Q6. Is x an even integer?

- 1) x is the square of an integer
- 2) x is the cube of an integer

Q7. If x and y are the integers between 10 and 99, inclusive. Is $\frac{x-y}{9}$ an integer?

- 1) x and y have the same two digits, but in reverse order.
- 2) The tens digit of x is 2 more than the units digit and the tens digit of y is 2 less than the units digit.

Q8. How many distinct prime factors does $5^{40} + 5^{37}$ have?

- A) 1
- B) 2
- C) 3
- D) 4
- E) 5

Q9. If r , s and t are consecutive integers, what is the greatest prime factor of $3^r + 3^s + 3^t$?

- A) 3
- B) 5
- C) 7
- D) 11
- E) 13

Q10. What is the sum of digits of the number $10^{50} - 74$?

- A) 9
- B) 18
- C) 27
- D) 36
- E) 440

Q11. If x , y and z are positive integers such that ' x ' is a factor of ' y ' and x is a multiple of ' z '. Which of the following is NOT necessarily an integer?

A) $\frac{x+z}{z}$

B) $\frac{y+z}{x}$

C) $\frac{x+y}{z}$

D) $\frac{xy}{z}$

E) $\frac{yz}{x}$

Q12. Is the integer z divisible by 6?

- 1) The greatest common factor of z and 12 is 3.
- 2) The greatest common factor of z and 15 is 15.

Q13. If x and y are perfect squares, then which of the following is not necessarily a perfect square?

A) x^2

B) xy

C) $4x$

D) $x+y$

E) x^5

Q14. If p and q are positive integers, how many integers are larger than pq and smaller than $p(q+2)$?

A) 3

B) $p+2$

C) $p-2$

D) $2p-1$

E) $2p+1$

Q15. If $x > y > 0$, which of the following must be true?

- I. $\frac{x+1}{y+1} > \frac{x}{y}$
- II. $\frac{x+1}{y+1} = \frac{x}{y}$
- III. $\frac{x+1}{y+1} > 1$

- A) I only
- B) II only
- C) III only
- D) I and II only
- E) II and III only

Q16. If 2 is the greatest number that will divide evenly into both x and y , what is the greatest number that will divide evenly into both $5x$ and $5y$?

- A) 2
- B) 4
- C) 6
- D) 8
- E) 10

Q17. If p divided by 9 leaves a remainder of 1, which of the following must be true?

- I. p is even
- II. p is odd
- III. $p = 3z + 1$, for some integer z

- A) I only
- B) II only
- C) III only
- D) I and II only
- E) None of the above

Q18. If the sum of two prime numbers x and y is odd, then the product of x and y must be divisible by

- A) 2
- B) 3
- C) 4
- D) 5
- E) 8

Q19. If $\frac{x+y}{x-y} = 3$ and x and y are integers, then which one of the following must be true?

- A) x is divisible by 4
- B) y is odd
- C) y is even
- D) x is even
- E) x is irreducible fraction

Q20. If y is an odd integer and the product of x and y equals 222, what is the value of x ?

- 1) x is a prime number
- 2) y is a three digit number

Q21. If x and y are prime numbers such that $x > y > 2$, then $x^2 - y^2$ must be divisible by which one of the following numbers?

- A) 3
- B) 4
- C) 5
- D) 9
- E) 12

Q22. If the positive integer N is a perfect square, which of the following must be true?

- I. Number of distinct factors of N is odd
- II. Sum of distinct factors of N is odd
- III. The number of distinct prime factors of N is even

- A) I only
- B) II only
- C) I and II only
- D) I and III only
- E) I, II and III

Q23. In a certain game, a large bag is filled with blue, green, purple and red chips worth 1, 5, x and 11 points each, respectively. The purple chips are worth more than the green chips but less than the red chips. A certain number of chips are then selected from the bag. If the product of the point values of selected chips is 88,000, how many purple chips were selected?

- A) 1
- B) 2
- C) 3
- D) 4
- E) 5

Q24. Is the positive integer x a perfect square?

- 1) The number of distinct factors of x is even
- 2) The sum of all distinct factors of x is even

Q25. Let a = sum of integers from 1 to 20 and b = sum of integers from 21 to 40. What is the value of $b - a$?

- A) 21
- B) 39
- C) 200
- D) 320
- E) 400

Q26. Does $x - y = 0$?

- 1) $\frac{x}{y} > 0$
- 2) $x^2 = y^2$

Q27. If p and q are integers, is $pq + 1$ even?

- 1) If p is divided by 2, the remainder is 1
- 2) If q is divided by 6, the remainder is 1

Q28. S is a set of integers such that

- I. If x is in S , then $-x$ is in S
- II. If both x and y are in S , then so is $x + y$.

Is -2 in S ?

- 1) 1 is in S
- 2) 0 is in S

Q29. A botanist select n^2 trees on an island and studies $(2n + 1)$ trees everyday where n is an even integer. He does not study the same tree twice. Which of the following cannot be the number of trees that he studies on the last day?

- A) 13
- B) 17
- C) 28
- D) 31
- E) 79

Q30. If $x = 2891 \times 2892 \times 2893 \times \dots \times 2898 \times 2899 \times 2900$, the what is the remainder when x is divided by 17?

- A) 0
- B) 4
- C) 7
- D) 10
- E) 14

Q31. For every positive integer n , the function $h(n)$ is defined to be the product of all the even integers from 2 to n , inclusive. If p is the smallest factor of $h(100) + 1$, then p is

- A) Between 2 and 10
- B) Between 11 and 20
- C) Between 21 and 30
- D) Between 31 and 40
- E) Greater than 40

Q32. If the sum of five consecutive positive integers is A , then the sum of the next five consecutive integers in terms of A is

- A) $A + 1$
- B) $A + 5$
- C) $A + 25$
- D) $2A$
- E) $5A$

Q33. A, B, C and D are all different digits between 0 and 9. If $AB + DC = 7B$ (AB, DC and $7B$ are two digit numbers), what is the value of C ?

- A) 0
- B) 1
- C) 2
- D) 3
- E) 5

Q34. If $2x < y$ and $2x^2 > xy$, which of the following must be true?

- A) $x > 1$
- B) $x < 0$
- C) $x > 0$
- D) $y < 0$
- E) $y > 1$

Q35. If x and y are different positive integers and $3x + y = 14$, what is the product of all the possible values of x ?

- A) 6
- B) 8
- C) 14
- D) 20
- E) 24

Q36. If x is an integer and $(\sqrt{x} \times x) - x = a$, which of the following must be true?

- I. a is even
 - II. a is positive
 - III. a is an integer
- A) I only
 - B) II only
 - C) III only
 - D) I and II only
 - E) None of the above

Q37. Which of the following expressions has the greatest value? (numbers)(650-750)

- A) $\frac{1876452}{1876455}$
- B) $\frac{1883446}{1883449}$
- C) $\frac{1883453}{1883456}$
- D) $\frac{1883456}{1883459}$
- E) $\frac{1883491}{1883494}$

Q38. If ' m ' and ' n ' are integers then what is the smallest possible value of integer m such that $\frac{m}{n} = 0.3636363636\dots\dots$?

- A) 3
- B) 4
- C) 7
- D) 13
- E) 22

Q39. If $N = 1234@$ and $@$ represents the units digit. Is N a multiple of 5? (numbers)(600-700)

- 1) $@!$ is not divisible by 5
- 2) $@$ is divisible by 9

Q40. If $(|p|!)^p = |p|!$, which of the following could be the value(s) of p ?

- A) -1
- B) 0
- C) 1
- D) -1 and 1
- E) -1, 0 and 1

Q41. If $5x = y + 7$, is $(x - y) > 0$?

- 1) $xy = 6$
- 2) x and y are consecutive integers with the same sign

Q42. If ' s ' and ' t ' are positive integer such that $\frac{s}{t} = 64.12$, which of the following could be the remainder when ' s ' is divided by ' t '?

- A) 2
- B) 4
- C) 8
- D) 20
- E) 45

Q43. If ' x ' is positive, which of the following could be the correct ordering of $\frac{1}{x}$, $2x$ and x^2 ?

- I. $x^2 < 2x < \frac{1}{x}$
- II. $x^2 < \frac{1}{x} < 2x$
- III. $2x < x^2 < \frac{1}{x}$

- A) None of the above
- B) I only
- C) III only
- D) I and II only
- E) II and III only

Q44. If p is a prime number greater than 2, what is the value of p ?

- 1) There are total of 100 prime numbers between 1 and $p + 1$.
- 2) There are a total of ' p ' prime numbers between 1 and 3912

Q45. If a, b and c are positive integers and are assembled into the six digit number abcabc, which of the following must be a factor of abcabc?

- A) 16
- B) 13
- C) 5
- D) 3
- E) None of the above

Q46. What is the remainder when $1^1 + 2^2 + 3^3 + \dots + 10^{10}$ is divided by 5?

- A) 0
- B) 1
- C) 2
- D) 3
- E) 4

Q47. If Q and T are integers, what is the value of Q?

- 1) $Q = \frac{2T}{7}$
- 2) $\frac{T+7}{2} = \frac{7(Q+2)}{4}$

Q48. If 'm' and 'n' are integers and $\sqrt{mn} = 10$, which of the following cannot be a value of $m + n$?

- A) 25
- B) 29
- C) 50
- D) 52
- E) 101

Q49. The three digits of a number add upto 11. The number is divisible by 5. The leftmost digit is double the middle digit. What is the product of the three digits?

- A) 40
- B) 72
- C) 78
- D) 88
- E) 125

Q50. If $x = y + y^2$ and y is a negative integer, when y decreases in value, then x

- A) Increases in value
- B) Fluctuates
- C) Decreases in value
- D) Remains the same
- E) Decreases in constant increments

Q51. If w, x, y and z are the digits of the four digit number N , a positive integer, what is the remainder when N is divided by 9?

- 1) $w + x + y + z = 13$
- 2) $N + 5$ is divisible by 9

Q52. If both ' x ' and ' y ' are positive integers less than 100 and greater than 10, is the sum ' $x + y$ ' a multiple of 11?

- 1) $(x - y)$ is a multiple of 22
- 2) The tens digit and the units digit of ' x ' are the same; the tens digit and units digit of ' y ' are the same

Q53. Susie can buy apples from two stores: a supermarket that sells apples only in bundles of 4 and a convenience store that sells single, unbundled apples. If Susie wants to ensure that the total number of apples she buys is a multiple of 5, then what is the minimum number of apples she must buy from the convenience store?

- A) 0
- B) 1
- C) 2
- D) 3
- E) 4

Q54. ' x ' is the sum of ' y ' consecutive integers, ' w ' is the sum of ' z ' consecutive integers. If $y = 2z$, and y and z are both positive integers, then each of the following could be true EXCEPT

- A) $x = w$
- B) $x > w$
- C) (x/y) is an integer
- D) (w/z) is an integer
- E) (x/z) is an integer

Q55. If ' x ' is a positive integer, is ' x ' prime? (prime numbers) (700-800)

- 1) ' x ' has the same number of factors as y^2 , where y is a positive integer greater than 2
- 2) ' x ' has the same number of factors as ' z ', where ' z ' is a positive integer greater than 2

Q56. The greatest common factor of 16 and the positive integer ' n ' is 4 and the greatest common factor of ' n ' and 45 is 3. Which of the following could be the greatest common factor of ' n ' and 210?

- A) 3
- B) 14
- C) 30
- D) 42
- E) 70

Q57. If integer k is equal to the sum of all even multiples of 15 between 295 and 615, what is the greatest prime factor of k ?

- A) 5
- B) 7
- C) 11
- D) 13
- E) 17

Q58. If 'a' and 'b' are positive integers such that $\left(\frac{a}{b}\right) = 2.86$, which of the following must be a divisor of 'a'?

- A) 10
- B) 13
- C) 18
- D) 26
- E) 50

Q59. If 'a' and 'b' are positive integers divisible by 6, is 6 the greatest common divisor of 'a' and 'b'?

- 1) $a = 2b + 6$
- 2) $a = 3b$

Q60. Is $x < z$?

- 1) $x = \left(\frac{1}{2}\right)y$
- 2) $y = 0.5z$

Q61. If x and y are integers such that $x < y < 0$, what is the value of $x - y$?

- 1) $(x + y)(x - y) = 5$
- 2) $xy = 6$