

# STONECOLD'S MATH CHALLENGE - PS AND DS QUESTION COLLECTION.

1) If  $z$  is divisible by all the integers from 1 to 5 inclusive, what is the smallest value of  $z$ ?

2) Data Sufficiency -> Is the positive integer  $z$  divisible by 12?

A)  $z$  is divisible by 3.

B)  $z$  is not divisible by 2.

3) Data Sufficiency -> Is integer  $z$  divisible by 21?

A)  $z$  is divisible by 7.

B)  $z$  is divisible by 3.

4) Data Sufficiency -> Is integer  $z$  divisible by 48?

A)  $z$  is divisible by 12.

B)  $z$  is divisible by 4.

5) Data Sufficiency -> Is integer  $z$  divisible by 12?

A)  $z$  is divisible by 8.

B)  $z$  is divisible by 6.

6) Data Sufficiency -> Is integer  $z$  divisible by 24?

**A)z is divisible by 6.**

**B)z is divisible by 4.**

**7)How many prime numbers between 1 and 100 are factors of 168?**

**8)How many Prime factors does 2180 have?**

**9)What is the greatest prime factor of  $4919-735$**

**A)2**

**B)3**

**C)7**

**D)13**

**E)19**

**10)If n is the product of integers from 1 to 12 exclusive,how many prime factors does n have?**

**11)If 2,3,5 are the prime factors of N,what is the value of N?**

**A)2**

**B)3**

**C)5**

**D) $2*3*5$**

**E)cannot be determined.**

12) If 2, 3, 5 are the "ONLY" prime factors of K, what is the value of K?

A) 2

B) 3

C) 5

D)  $2 \cdot 3 \cdot 5$

E) cannot be determined.

13) Data Sufficiency -> What is the value of positive integer K?

A) 2, 5, 7 are prime factors of K.

B)  $K < 100$

14) If p is a positive integer and 200 multiplied by p is square of an integer, what is the value of p?

A) 2

B) 3

C) 5

D) 10

E) Cannot be determined.

15) Data Sufficiency -> What is the value of positive integer p?

A) 200 multiplied by p is square of an integer.

B) p is an even number less than 15.

16) Data Sufficiency -> What is the value of positive integer p?

A) 300 multiplied by p is square of an integer.

B) p is an even number less than 15.

17)  $10^{25} - 560$  is divisible by all of the following EXCEPT:-

**A)11**

**B)8**

**C)5**

**D)4**

**E)3**

**18)Data Sufficiency->What is the value of positive integer p?**

**A)300 multiplied by p is square of an integer.**

**B)p is a factor of 75**

**19)Data Sufficiency->What is the value of positive integer p?**

**A)200 multiplied by p is square of an integer.**

**B)p is a factor of 60.**

**20)Data sufficiency-> If a and b are prime numbers,what is the value of a\*b?**

**A)a-b=1**

**B)a=3**

**21)If x and y are prime numbers, each greater than 2, which of the following must be true?**

**I. x+y is an even integer**

**II. xy is an odd integer**

**III.  $(x/y)$  is not an integer**

- A. II only**
- B. I and II only**
- C. I and III only**
- D. II and III only**
- E. I, II, and III**

**22) Which of the following statements must be true ->**

- A) zero is neither prime nor composite.**
- B) one is neither prime nor composite.**
- C) -3 and 3 are both primes.**

**23) Which of the following statements must be true ->**

- 1) A prime number must be positive.**
- 2) For any prime number  $p$ , there is no  $x$  such that  $1 < x < p$  and  $x$  is a divisor of  $p$ .**
- 3) The product of first ten primes is even.**
- 4) All prime numbers greater than 71 are odd.**
- 5) 2 and 3 are the only consecutive integers that are also prime numbers.**
- 6)  $p$  is a prime number and  $x$  and  $y$  are positive integers. If  $p = x * y$  then one out of  $x$  or  $y$  must be one.**
- 7) All the prime numbers greater than 3 can be written as either  $4n + 1$  or  $4n - 1$ .**
- 8) All the prime numbers greater than 3 can be written as either  $6n + 1$  or  $6n - 1$ .**

**24) Data Sufficiency -> If  $p$  is a prime number, what is the value of  $p$ ?**

**A)  $11 < p < 17$**

**B)  $p$  is divisible by 13.**

**25) Data Sufficiency -> If  $A$  and  $B$  are positive integers, is  $A/B$  an integer?**

**(1) Every factor of  $B$  is also a factor of  $A$ .**

**(2) Every prime factor of  $B$  is also a prime factor of  $A$ .**

**26) Data Sufficiency -> Is  $n/14$  an integer?**

**(1)  $n$  is divisible by 28.**

**(2)  $n$  is divisible by 70.**

**27) If  $x$  is a prime number, what is the value of  $x$ ?**

**(1) There are a total of 50 prime numbers between 71 and  $x$ , inclusive.**

**(2) There is no integer  $n$  such that  $x$  is divisible by  $n$  and  $1 < n < x$ .**

**28) Data Sufficiency -> If  $p = (n)(5^x)(3^k)$ , is  $p$  divisible by 10?**

**(1)  $n$ ,  $x$ , and  $k$  are even.**

**(2)  $x > n > k > 0$**

**29) Data Sufficiency -> If  $x$  is a prime number, what is the value of  $x$ ?**

**1) There are 3 prime numbers between 11 and  $x$**

**2)  $x+1$  is a prime number**

**30) If  $A$  is a positive integer, then  $A$ ,  $A^3$  and  $A^7$  will have the exact same prime factors.**

**A) True**

**B) False**

**31) Data Sufficiency -> If  $y$  and  $x$  are positive integers, is  $y$  divisible by 3?**

**(1)  $y = x(x+1)$**

**(2)  $y^2$  is divisible by 9.**

**32) Data Sufficiency -> If  $y$  and  $x$  are positive integers, is  $y$  divisible by  $x$ ?**

**(1)  $y = x^2 + x$**

**(2)  $x$  has the same prime factors as  $y$ .**

**33) Data Sufficiency -> If  $z$  is a positive integer, is  $(z^{31}+7)^2$  divisible by 4?**

**A)  $\sqrt{z}$  has five prime factors.**

**B) All prime factors of  $z^3$  are greater than 7.**

**34) If  $x$  is a positive odd integer and  $y$  is a negative even integer, which of the following must be true?**

- A.  $x^3 + y$  is a positive odd integer**
- B.  $x^2 + y^2$  is a negative odd integer**
- C.  $x^0 + y^{11}$  is a negative odd integer**
- D.  $x + y$  is a positive odd integer**
- E.  $x + y$  is a negative odd integer**

**35) Data Sufficiency -> How many positive prime numbers are less than the integer  $n$ ?**

- (1)  $14 < n < 20$**
- (2)  $13 < n < 17$**

**36) Data Sufficiency -> If  $x$  and  $y$  are positive integers, is  $x$  divisible by  $y$ ?**

- 1)  $x$  is divisible by 5.**
- 2)  $y$  is divisible by 5.**

**37) Data Sufficiency -> How many prime factors does  $x^{37}$  have?**

- (1) The number of prime factors of  $16x$  is one more than the number of prime factors of  $x^4$**
- (2)  $2x^{16}$  has 2 prime factors**

**38) If a positive integer  $x$  has 3 prime factors, how many prime factors does  $x^3$  have?**

**A) 27**

**B) 6**

**C) 3**

**D) 1**

**E) cannot be determined**

**39) Data Sufficiency -> If  $k$  is a positive integer, how many unique prime factors does  $14k$  have?**

**(1)  $k^4$  is divisible by 100**

**(2)  $50 \cdot k$  has 2 prime factors**

**40) Data Sufficiency -> If  $x$  is an integer, is  $x^3$  divisible by 9?**

**(1)  $x^2$  is divisible by 9.**

**(2)  $x^4$  is divisible by 9.**

**41) Data sufficiency -> How many different prime numbers are factors of positive integer  $n$ ?**

**(1) 4 different prime numbers are factors of  $2n$**

**(2) 4 different prime numbers are factors of  $n^2$**

**42) If  $x$  and  $y$  are positive integers, are they consecutive?**

**1)  $x+y=3$**

**2)  $x - y = 1$**

**43) Data Sufficiency -> Is the integer  $r$  divisible by 3?**

- (1)  $r$  is the product of 4 consecutive integers.**
- (2)  $r < 25$**

**44) Data Sufficiency -> Is  $x^2 * y^4$  an integer divisible by 9?**

- (1)  $x$  is an integer divisible by 3.**
- (2)  $xy$  is an integer divisible by 9.**

**45) Data Sufficiency -> For positive integers  $x$  and  $y$ ,  $x^2 = 350y$ . Is  $y$  divisible by 28?**

- (1)  $x$  is divisible by 4.**
- (2)  $x^2$  is divisible by 28.**

**46) Data Sufficiency -> How many Prime factors does positive integer  $n$  have?**

- A)  $n^3$  has 7 prime factors.**
- B)  $\sqrt{n}$  has 7 prime factors.**

**47) If  $x$  and  $y$  represent the number of factors of 90 and 147 respectively. What is the value of  $x - y$ ?**

**48) If  $n$  is the product of all the integers from 1 to 10 exclusive, how many factors does  $n$  have?**

**49)How many even factors does 21600 have?**

**A)32**

**B)42**

**C)60**

**D)25**

**E)52**

**50)How many positive odd divisors does 540 have?**

**A)6**

**B)8**

**C)12**

**D)15**

**E)24**

**51)How many of the factors of 72 are divisible by 2?**

**A)4**

**B)5**

**C)6**

**D)8**

**E)9**

**52)The number  $100^2$  has how many factors?**

**A) 28**

**B) 25**

**C) 24**

**D) 20**

**E) 16**

**53)How many factors of 330 are odd numbers greater than 1?**

**A)8**

**B)7**

**C)6**

**D)5**

**E)4**

**54)If  $N=27 * 35 * 56 * 78$ . How many factors of N are divisible by 50 but NOT by 100?**

**A)240**

**B)345**

**C)270**

**D)120**

**E)None of these**

**55)Data Sufficiency->How many positive factors does the positive integer x have?**

**(1) x is the product of 3 distinct prime numbers.**

**(2) x and 37 have the same number of positive factors.**

**56)Data Sufficiency->How many factors does x have, if x is a positive integer?**

**(1)  $x=pn$ , where p is a prime number**

**(2)  $nn=n+n$ , where n is a positive integer**

**57)Data Sufficiency->If 2,3,5 are the only prime factors of a positive integer p,what is the value of p?**

**A) $p>100$**

**B)p has exactly 12 factors including 1 and 12.**

**58)Data Sufficiency->Is the positive integer P prime?**

**(1)  $61<P<67$**

**(2) P is not divisible by 2.**

**59) Which of the following statements is/are true?**

**A) A perfect square always has an odd number of factors.**

**B) If a given integer has an odd number of factors then that integer must be a perfect square.**

**60) How many factors does 64 have?**

**A) 8**

**B) 6**

**C) 7**

**D) 6**

**E) 4**

**61) Data Sufficiency -> Is the positive integer  $n$  divisible by 6?**

**(1)  $n^2 + 180$  is an integer.**

**(2)  $144n^2$  is an integer**

**62) If a positive integer  $x$  has 5 prime factors, how many prime factors does  $3x$  have?**

**A) 5**

**B) 6**

**C) 8**

**D) 15**

**E) cannot be determined**

**63) How many positive distinct prime factors does  $5^{20} + 5^{17}$  have?**

**A) One**

**B) Two**

**C) Three**

**D) Four**

**E) Five**

**64) How many prime numbers exist between 200 and 220?**

- (A) None
- (B) One
- (C) Two
- (D) Three
- (E) Four

**65) Data Sufficiency -> If  $y$  is a positive odd integer less than 33, does  $y$  have a factor  $p$  such that  $1 < p < y$ ?**

- A)  $y+2$  is divisible by 3.**
- B) Units digit of  $y$  is 7.**

**66) If  $x$  is a positive integer less than 100, for how many values of  $x$  is  $x/6$  a prime number?**

- A) 2**
- B) 6**
- C) 8**
- D) 13**
- E) 17**

**67) Data Sufficiency -> If  $n$  is an integer between 10 and 99, is  $n < 80$ ?**

- (1) The sum of the two digits of  $n$  is a prime number.**
- (2) Each of the two digits of  $n$  is a prime number.**

**68) If  $n$  is a positive integer, which of the following statements are correct?**

- A) All the prime numbers greater than 3 can be represented in the form  $4n + 1$  or  $4n + 3$ .**
- B) All numbers of the form  $4n + 1$  and  $4n + 3$  are prime numbers.**
- C) All the prime numbers greater than 3 can be represented in the form  $6n - 1$  or  $6n + 1$ .**
- D) All numbers of the form  $6n + 1$  and  $6n - 1$  are prime numbers.**

**69) Data Sufficiency -> If  $p$  is an integer, is  $p + 4$  a prime number less than 50?**

**(1)  $p + 1$  is a prime number.**

**(2)  $p$  is a prime number.**

**70) How many odd factors does the number 2100 have?**

**A) 36**

**B) 24**

**C) 12**

**D) 8**

**E) cannot be determined.**

**71) Data Sufficiency -> If  $p$  is an integer greater than 1, is  $p$  a prime number?**

**(1)  $p$  is a factor of 13.**

**(2)  $p$  is a factor of 78.**

**72) If the number 13 completely divides  $x$ , and  $x = a^2 * b$ , where  $a$  and  $b$  are distinct prime numbers, which of these numbers must be divisible by 169?**

**A)  $a^2$**

**B)  $b^2$**

**C)  $a * b$**

**D)  $a^2 * b^2$**

**E)  $a^3 * b$**

**73) Data sufficiency -> If  $p$  is an integer and  $p > 1$ , is  $p$  a prime number?**

**A)  $p$  has  $p$  factors.**

**B)  $p$  is a factor of 26.**

**74) Data Sufficiency -> Is the number of distinct prime factors of the positive integer  $N$  more than 4?**

**(1)  $N$  is a multiple of 42.**

**(2)  $N$  is a multiple of 98**

**75)Data Sufficiency->If  $k$  is a positive integer, how many different prime factors does  $k$  have?**

**(1)  $k/30$  is an integer**

**(2)  $k < 100$**

**76)Data Sufficiency->If  $k$  is a positive integer, how many different prime factors does  $k$  have?**

**(1)  $k/60$  is an integer**

**(2)  $k < 100$**

**77)Data Sufficiency->If  $A$  and  $B$  are positive integers, does  $A$  have more prime factors than  $B$ ?**

**(1)  $B$  is the square root of  $A$**

**(2)  $A \div B$  is an integer**

**78)What is the greatest prime factor of  $123-96$  ?**

**A)2**

**B)3**

**C)7**

**D)17**

**E)19**

**79)What is the greatest prime factor of  $4^{17} - 2^{28}$ ?**

**A)2**

**B)3**

**C)5**

**D)7**

**E)11**

**80)What is the total number of distinct prime factors of 28980?**

**A)2**

**B)3**

**C)4**

**D)5**

E)6

81)What is the greatest prime factor of  $3^6 - 1$  ?

A. 2

B. 3

C. 7

D. 13

E. 17

82)Find the number of factors of 180 that are in the form  $(4*k + 2)$ , where k is a non-negative integer?

A)1

B)2

C)3

D)4

E)6

83)Data Sufficiency->If A and B are positive integers, does B have more prime factors than A?

(1) B is the square root of A

(2)  $A \div B$  is an integer

84)If  $N = 10!$  then what is the minimum number which should be multiplied with N to make it a perfect square?

A)7

B)14

C)21

D)28

E)36

85)If  $N = 22 * 33 * 55$ , find the total number of odd and even factors of N.

A)24,96

**B)15,30**

**C)24,48**

**D)15,96**

**E)15,48**

**86)Which of the following numbers is a prime number?**

**A)2343**

**B)3457**

**C)4689**

**D)7731**

**E)9861**

**87)The product of all the prime numbers less than 20 is closest to which of the following powers of 10 ?**

**(A) 10<sup>9</sup>**

**(B) 10<sup>8</sup>**

**(C) 10<sup>7</sup>**

**(D) 10<sup>6</sup>**

**(E) 10<sup>5</sup>**

**88)If n is the product of the integers from 1 to 8, inclusive, how many different prime factors greater than 1 does n have?**

**(A) four**

**(B) five**

**(C) six**

**(D) seven**

**(E) eight**

**89)Find the number of factors of 240 that are in the form  $(4 \cdot p + 2)$ , where p is a non-negative integer?**

**A)1**

**B)2**

**C)3**

**D)4**

**E)5**

**90)Data Sufficiency->What is the value of the integer p ?**

**(1) Each of the integers 2, 3, and 5 is a factor of p.**

**(2) Each of the integers 2, 5, and 7 is a factor of p.**

**91)Data Sufficiency->Does the integer k have at least three different positive prime factors?**

**(1)  $k/15$  is an integer.**

**(2)  $k/10$  is an integer.**

**92)If p is the product of the integers from 1 to 30, inclusive, what is the greatest integer k for which  $3^k$  is a factor of p?**

**A. 10**

**B. 12**

**C. 14**

**D. 16**

**E. 18**

**93)If  $n = 20! + 17$ , then n is divisible by which of the following?**

**I. 15**

**II. 17**

**III. 19**

**(A) None**

**(B) I only**

**(C) II only**

**(D) I and II**

**(E) II and III**

**94)If  $3 < x < 100$ , for how many values of x is  $x/3$  the square of a prime number?**

**(A) Two**

- (B) Three
- (C) Four
- (D) Five
- (E) Nine

95) How many integer values are there for  $x$  such that  $1 < 3x + 5 < 17$ ?

- A) Two
- B) Three
- C) Four
- D) Five
- E) Six

96) For any positive integer  $n$ , the sum of the first  $n$  positive integers equals  $n(n+1)/2$ . What is the sum of all the even integers between 99 and 301?

- A. 10,100
- B. 20,200
- C. 22,650
- D. 40,200
- E. 45,150

97) If the sum of the first  $n$  positive integers is  $S$ , what is the sum of the first  $n$  positive even integers, in terms of  $S$ ?

- (A)  $S/2$
- (B)  $S$
- (C)  $2S$
- (D)  $2S + 2$
- (E)  $4S$

98) How many prime numbers between 1 and 100 are factors of 7,150?

- (A) One

**(B) Two**

**(C) Three**

**(D) Four**

**(E) Five**

**99) If  $n$  is a prime number between 0 and 100, how many positive divisors does  $n^3$  have?**

**A) 1**

**B) 2**

**C) 3**

**D) 4**

**E) 5**

**100) If  $y$  is the smallest positive integer such that 3,150 multiplied by  $y$  is the square of an integer, then  $y$  must be**

**A) 2**

**B) 5**

**C) 6**

**D) 7**

**E) 14**