

1. The sum of n consecutive positive integers is 45. What is the value of n ?

- (1) n is even
- (2) $n < 9$

(1) $n=2 \rightarrow 22+23=45$, $n=4 \rightarrow n=6 \ x_1+(x_1+1)+(x_1+2)+(x_1+3)+(x_1+4)+(x_1+5)=45 \ x_1=5$. At least two options for n . Not sufficient.

(2) $n < 9$ same thing not sufficient.

(1)+(2) No new info. Not sufficient.

Answer: E.

2. Is a product of three integers XYZ a prime?

- (1) $X=-Y$
- (2) $Z=1$

(1) $x=-y \rightarrow$ for xyz to be a prime z must be $-p$ AND $x=-y$ shouldn't be zero. Not sufficient.

(2) $z=1 \rightarrow$ Not sufficient.

(1)+(2) $x=-y$ and $z=1 \rightarrow x$ and y can be zero, $xyz=0$ not prime OR xyz is negative, so not prime. In either case we know xyz not prime.

Answer: C

3. Multiplication of the two digit numbers wx and cx , where w, x and c are unique non-zero digits, the product is a three digit number. What is $w+c-x$?

(1) The three digits of the product are all the same and different from w, c and x .

(2) x and $w+c$ are odd numbers.

(1) $wx+cx=aaa$ (111, 222, ... $999=37*k$) \rightarrow As x is the units digit in both numbers, a can be 1,4,6 or 9 (2,3,7 out because x^2 can not end with 2,3, or 7. 5 is out because in that case x also should be 5 and we know that x and a are distinct numbers).

1 is also out because $111=37*3$ and we need 2 two digit numbers.

$444=37*12$ no good we need units digit to be the same.

$666=37*18$ no good we need units digit to be the same.

$999=37*27$ is the only possibility all digits are distinct except the unit digits of multiples.

Sufficient

(2) x and $w+c$ are odd numbers.

Number of choices: 13 and 23 or 19 and 29 and $w+c-x$ is the different even number.

Answer: A.

4. Is $y - x$ positive?

- (1) $y > 0$
- (2) $x = 1 - y$

Easy one even if $y > 0$ and $x+y=1$, we can find the x, y when $y-x > 0$ and $y-x < 0$

Answer: E.

5. If a and b are integers, and $a \neq b$, is $|a|b > 0$?

- (1) $|a^b| > 0$
- (2) $|a|^b$ is a non-zero integer

This is tricky $|a|b > 0$ to hold true: $a \neq 0$ and $b > 0$.

(1) $|a^b| > 0$ only says that $a \neq 0$, because only way $|a^b|$ not to be positive is when $a=0$. Not sufficient. NOTE having absolute value of variable $|a|$, doesn't mean it's positive. It's not negative $\rightarrow |a| > 0$

(2) $|a|^b$ is a **non-zero integer**. What is the difference between (1) and (2)? Well this is the tricky part: (2) says that $a \neq 0$ and plus to this gives us two possibilities as it states that it's **integer**:

A. $-1 > a > 1$ ($|a| > 1$), on this case b can be any positive integer: because if b is negative $|a|^b$ can not be integer.

OR

B. $|a|=1$ ($a=-1$ or 1) and b can be any integer, positive or negative.

So (2) also gives us two options for b . Not sufficient.

(1)+(2) nothing new: $a \neq 0$ and two options for b depending on a . Not sufficient.

Answer: E.

6. If M and N are integers, is $(10^M + N)/3$ an integer?

- (1) $N = 5$

(2) MN is even

Note: it's not given that M and N are positive.

(1) $N=5 \rightarrow$ if $M>0$ $(10^M + N)/3$ is an integer $((1+5)/3)$, if $M<0$ $(10^M + N)/3$ is a fraction $((1/10^{|M|} + 5)/3)$. Not sufficient.

(2) MN is even \rightarrow one of them or both positive/negative AND one of them or both even. Not sufficient

(1)+(2) $N=5$ MN even \rightarrow still M can be negative or positive. Not sufficient.

Answer: E.

7. If b, c, and d are constants and $x^2 + bx + c = (x + d)^2$ for all values of x, what is the value of c?

(1) $d = 3$

(2) $b = 6$

Note this part: "for all values of x"

So, it must be true for $x=0 \rightarrow c=d^2 \rightarrow b=2d$

(1) $d = 3 \rightarrow c=9$ Sufficient

(2) $b = 6 \rightarrow b=2d, d=3 \rightarrow c=9$ Sufficient

Answer: D.

8. If x and y are non-zero integers and $|x| + |y| = 32$, what is xy?

(1) $-4x - 12y = 0$

(2) $|x| - |y| = 16$

(1) $x+3y=0 \rightarrow$ x and y have opposite signs \rightarrow either $4y=32$ $y=8$ $x=-3$, $xy=-24$ OR $-4y=32$ $y=-8$ $x=3$ $xy=24$. The same answer. Sufficient.

(2) Multiple choices. Not sufficient.

Answer: A.

9. Is the integer n odd

(1) n is divisible by 3

(2) 2n is divisible by twice as many positive integers as n

(1) 3 or 6. Clearly not sufficient.

(2) TIP:

When odd number n is doubled, 2n has twice as many factors as n.

That's because odd number has only odd factors and when we multiply n by two we remain all these odd factors as divisors and adding exactly the same number of even divisors, which are $odd \cdot 2$.

Sufficient.

Answer: B.

10. The sum of n consecutive positive integers is 45. What is the value of n?

(1) n is odd

(2) $n \geq 9$

Look at the Q 1 we changed even to odd and $n < 9$ to $n \geq 9$

(1) not sufficient see Q1.

(2) As we have consecutive positive integers max for n is 9: $1+2+3+\dots+9=45$. (If $n > 9=10$ first term must be zero. and we are given that all terms are positive) So only case $n=9$. Sufficient.

Answer: B.